

A Novel Adaptive Beamformer for MEG Source Reconstruction Effective When Large Background Brain Activities Exist

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Abstract—This paper proposes a novel prewhitening eigenspace beamformer suitable for magnetoencephalogram (MEG) source reconstruction when large background brain activities exist. The prerequisite for the method is that control-state measurements, which contain only the contributions from the background interference, be available, and that the covariance matrix of the background interference can be obtained from such control-state measurements. The proposed method then uses this interference covariance matrix to remove the influence of the interference in the reconstruction obtained from the target measurements. A numerical example, as well as applications to two types of MEG data, demonstrates the effectiveness of the proposed method.

Index Terms—Adaptive beamforming, brain noise, magnetoencephalography, prewhitening, source reconstruction.

I. INTRODUCTION

ONE MAJOR problem with magnetoencephalogram (MEG) measurements is that measured MEG signal generally contains interfering magnetic fields generated from spontaneous brain activities. Such background interference degrades the quality of the source reconstruction results, and often make interpreting the reconstruction results difficult. Therefore, the background interference is sometimes referred to as brain noise or physiological noise. The degradation is particularly severe in adaptive beamformer source reconstruction methods [1], [2] because the high-rank nature of the background spontaneous activity [3], [4] may invalidate the underlying low-rank signal assumption necessary for formulating the adaptive beamformers. We show in Section III that the background brain activity can cause a significant reduction in the source intensity and severe spatial blur in adaptive-beamformer reconstruction results.

This paper proposes a novel prewhitening eigenspace beamformer, which can attain the source reconstruction free from the influence of background interference when a large amount of

background activity exists. The prerequisite for the proposed method is that control-state measurements, which contain only the contributions from the background interference, be available, and that the covariance matrix of the background interference can be obtained from such control-state measurements. The proposed method then uses this interference covariance matrix to remove the influence of the interference in the reconstruction results obtained from the target measurements where both signal and interference exist.

The proposed beamformer is particularly useful for reconstructing source activities that are stimulus-evoked but not time-locked to the stimulus. Since signals from such non-time-locked activities are generally averaged out through the epoch-averaging process, the beamformer weight should be derived using a covariance matrix obtained from nonaveraged raw epochs. However, the nonaveraged epochs generally contain a large amount of background interference whose amplitude is usually considerably larger than that of the evoked activity. Therefore, the successful reconstruction of nontime-locked activities requires removing the influence of the background interference. In Section IV-B, we show one such example in which primary hand-motor activation is clearly reconstructed as a result of applying the method to the motor-evoked field with a frequency band of 15–25 Hz. The result of this application demonstrates the effectiveness of the proposed method for reconstructing MEG source activities using nonaveraged raw epochs.

In this paper, we first present the analysis regarding the influence of the background interference on the adaptive beamformer source reconstruction in Section III. Then, the prewhitening eigenspace beamformer is proposed in Section IV. The proposed method is validated first by our computer simulation in Section V and then by applications to auditory and motor responses in Section VI. Throughout this paper, plain italics indicate scalars, lower-case boldface italics indicate vectors, and upper-case boldface italics indicate matrices. The eigenvalues are numbered in decreasing order.

II. ADAPTIVE-BEAMFORMER FOR NEUROMAGNETIC RECONSTRUCTION

A. Definitions

We define the magnetic field measured by the m th detector coil at time t as $b_m(t)$, and a column vector $\mathbf{b}(t) = [b_1(t), b_2(t), \dots, b_M(t)]^T$ as a set of measured data

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where M is the total number of detector coils and superscript T indicates the matrix transpose. The spatial location is represented by a three-dimensional (3-D) vector $\mathbf{r} : \mathbf{r} = (x, y, z)$. The covariance matrix of the measurement is denoted as \mathbf{R} , i.e., $\mathbf{R} = \langle \mathbf{b}(t)\mathbf{b}^T(t) \rangle$ where $\langle \cdot \rangle$ indicates the ensemble average, which is replaced with the time average over a certain time window in practice. The moment magnitude of a source at \mathbf{r} is denoted as $s(\mathbf{r}, t)$. The orientation of the source at \mathbf{r} is defined as a 3-D vector $\boldsymbol{\eta}(\mathbf{r}) = [\eta_x(\mathbf{r}), \eta_y(\mathbf{r}), \eta_z(\mathbf{r})]^T$ whose ζ component, (where ζ equals $x, y,$ or z), is equal to the cosine of the angle between the direction of the source moment and the ζ direction. We define $l_m^\zeta(\mathbf{r})$ as the output of the m th sensor; the output is induced by a unit-magnitude source located at \mathbf{r} and directed in the ζ direction. The column vector $\mathbf{l}_\zeta(\mathbf{r})$ is defined as $\mathbf{l}_\zeta(\mathbf{r}) = [l_1^\zeta(\mathbf{r}), l_2^\zeta(\mathbf{r}) \cdots l_M^\zeta(\mathbf{r})]^T$. The lead field matrix, which represents the sensitivity of the whole sensor array at \mathbf{r} , is defined as $\mathbf{L}(\mathbf{r}) = [\mathbf{l}_x(\mathbf{r}), \mathbf{l}_y(\mathbf{r}), \mathbf{l}_z(\mathbf{r})]$. The lead-field vector in the source-moment direction is defined as $\mathbf{l}(\mathbf{r})$ where $\mathbf{l}(\mathbf{r}) = \mathbf{L}(\mathbf{r})\boldsymbol{\eta}(\mathbf{r})$.

B. Adaptive Beamformer Source Reconstruction

To solve neuromagnetic source reconstruction problems, we focus on the class of methods referred to as the adaptive beamformer, which was originally developed in the field of array signal processing [5]. The beamformer estimates the source current density by computing $\hat{\mathbf{s}}(\mathbf{r}, t) = \mathbf{w}^T(\mathbf{r})\mathbf{b}(t)$ where $\hat{\mathbf{s}}(\mathbf{r}, t)$ is the estimated source magnitude. The column vector $\mathbf{w}(\mathbf{r})$ expresses a set of filter weights. The weight vector of the minimum-variance beamformer, which is the best-known adaptive beamformer, is expressed as

$$\mathbf{w}(\mathbf{r}) = \frac{\mathbf{R}^{-1}\mathbf{l}(\mathbf{r})}{\mathbf{l}^T(\mathbf{r})\mathbf{R}^{-1}\mathbf{l}(\mathbf{r})} \quad (1)$$

where $\mathbf{l}(\mathbf{r})$ is defined as $\mathbf{l}(\mathbf{r}) = \mathbf{L}(\mathbf{r})\boldsymbol{\eta}_{opt}(\mathbf{r})^1$. Here, $\boldsymbol{\eta}_{opt}(\mathbf{r})$ is the optimum direction determined as the direction that gives the maximum beamformer outputs [7], [8]. Using the above weight, the reconstructed source power is expressed as

$$\langle \hat{\mathbf{s}}(\mathbf{r}, t)^2 \rangle = \frac{\mathbf{l}^T(\mathbf{r})\mathbf{R}^{-1}\langle \mathbf{b}(t)\mathbf{b}^T(t) \rangle\mathbf{R}^{-1}\mathbf{l}(\mathbf{r})}{[\mathbf{l}^T(\mathbf{r})\mathbf{R}^{-1}\mathbf{l}(\mathbf{r})]^2} = \frac{1}{\mathbf{l}^T(\mathbf{r})\mathbf{R}^{-1}\mathbf{l}(\mathbf{r})} \quad (2)$$

because $\langle \mathbf{b}(t)\mathbf{b}^T(t) \rangle = \mathbf{R}$

The minimum-variance beamformer can be extended to the eigenspace-projection beamformer, which is known to be tolerant of errors in the forward modeling or the estimation of the data covariance matrix [9]. The extension is attained by projecting the weight vector in (1) onto the signal subspace of the measurement covariance matrix. That is, redefining the weight vector in (1) as $\mathbf{w}_{MV}(\mathbf{r})$, the weight vector for the eigenspace-projection beamformer is obtained using

$$\mathbf{w}(\mathbf{r}) = \mathbf{E}_S\mathbf{E}_S^T\mathbf{w}_{MV}(\mathbf{r}). \quad (3)$$

¹In practice, the normalized lead field $\mathbf{l}(\mathbf{r})/\|\mathbf{l}(\mathbf{r})\|$ is often used in (1) to avoid artifacts caused by the variation of the lead field norm $\|\mathbf{l}(\mathbf{r})\|$ [6]. We use the normalized lead field in our experiments in Sections V and VI.

In this equation, \mathbf{E}_S is a matrix whose columns consist of the signal-level eigenvectors of \mathbf{R} , and $\mathbf{E}_S\mathbf{E}_S^T$ is the projection matrix that projects a vector onto the signal subspace of \mathbf{R} .

III. INFLUENCE OF BACKGROUND BRAIN ACTIVITY ON ADAPTIVE-BEAMFORMER RECONSTRUCTION

We use a model for the measurements $\mathbf{b}(t)$ expressed as

$$\mathbf{b}(t) = \mathbf{b}_s(t) + \mathbf{b}_I(t) + \mathbf{n}(t) \quad (4)$$

where $\mathbf{b}_s(t)$ is the magnetic field generated from the signal sources of interest, $\mathbf{b}_I(t)$ is the magnetic field generated by the background activity, and $\mathbf{n}(t)$ is the additive sensor noise. The spatial-filter outputs are then expressed as

$$\begin{aligned} \hat{\mathbf{s}}(\mathbf{r}, t) &= \mathbf{w}^T(\mathbf{r})\mathbf{b}(t) \\ &= \mathbf{w}^T(\mathbf{r})\mathbf{b}_s(t) + \mathbf{w}^T(\mathbf{r})\mathbf{b}_I(t) + \mathbf{w}^T(\mathbf{r})\mathbf{n}(t). \end{aligned} \quad (5)$$

For nonadaptive spatial filters, the influence of the interference $\mathbf{b}_I(t)$ is simply the overlap of $\mathbf{w}^T(\mathbf{r})\mathbf{b}_I(t)$ onto the reconstruction of the signal of interest, $\mathbf{w}^T(\mathbf{r})\mathbf{b}_s(t)$. For adaptive beamformers, however, the interference $\mathbf{b}_I(t)$ affects the source reconstruction results in a more complex manner because $\mathbf{b}_I(t)$ also affects the beamformer weight $\mathbf{w}(\mathbf{r})$ through the covariance matrix \mathbf{R} . In this section, we derive the resolution kernel of the minimum-variance beamformer, taking the background interference into account. Numerical examples of the resolution kernel are presented in Section V-A. These numerically-obtained kernels clearly show that the background activity can cause a significant source-intensity reduction as well as severe spatial blur in the adaptive-beamformer reconstruction results.

We define the background interference activity at the location \mathbf{r} and time t as $\xi(\mathbf{r}, t)$, and assume that the background sources are continuously distributed. Thus, we have

$$\mathbf{b}_I(t) = \int \xi(\mathbf{r}, t)\mathbf{l}(\mathbf{r})d\mathbf{r} \quad (6)$$

where the integral is taken over the whole source space. Let us also assume that only a single target source exists at \mathbf{r}_1 with an orientation equal to $\boldsymbol{\eta}_1$. The magnitude of the target source is denoted $s(\mathbf{r}_1, t)$. Then, defining \mathbf{f} such that $\mathbf{f} = \mathbf{L}(\mathbf{r}_1)\boldsymbol{\eta}_1$, the measurement $\mathbf{b}(t)$ is expressed as

$$\mathbf{b}(t) = s(\mathbf{r}_1, t)\mathbf{f} + \int \xi(\mathbf{r}, t)\mathbf{l}(\mathbf{r})d\mathbf{r} + \mathbf{n}(t). \quad (7)$$

The sensor noise $\mathbf{n}(t)$ can be modeled as white Gaussian noise uncorrelated between different sensor channels, and we can generally assume that the relationship $\langle \mathbf{n}(t)\mathbf{n}^T(t) \rangle = \sigma_0^2\mathbf{I}$ holds where σ_0^2 is the variance of the sensor noise and \mathbf{I} is the identity matrix. Therefore, the covariance matrix of the measurements is given by

$$\begin{aligned} \mathbf{R} &= \langle \mathbf{b}(t)\mathbf{b}^T(t) \rangle \\ &= \sigma_1^2\mathbf{f}\mathbf{f}^T + \int \int \langle \xi(\mathbf{r}, t)\xi(\mathbf{r}', t) \rangle \\ &\quad \times \mathbf{l}(\mathbf{r})\mathbf{l}^T(\mathbf{r}')d\mathbf{r}d\mathbf{r}' + \sigma_0^2\mathbf{I} \end{aligned} \quad (8)$$

where the signal power σ_1^2 is defined such that $\sigma_1^2 = \langle s(\mathbf{r}_1, t)^2 \rangle$. We also assume that the background source activity is spatially uniform and incoherent, i.e.,

$$\langle \xi(\mathbf{r}, t) \xi(\mathbf{r}', t) \rangle = \sigma_c^2 \delta(\mathbf{r} - \mathbf{r}') \quad (9)$$

where σ_c^2 is the power of the background source activity. Substituting (9) into (8), we obtain

$$\mathbf{R} = \sigma_1^2 \mathbf{f} \mathbf{f}^T + \sigma_c^2 \mathbf{G} + \sigma_0^2 \mathbf{I} \quad (10)$$

where \mathbf{G} is the gram matrix defined as

$$\mathbf{G} = \int \mathbf{l}(\mathbf{r}) \mathbf{l}^T(\mathbf{r}) d\mathbf{r}. \quad (11)$$

The resolution kernel of the minimum-variance beamformer for a point source at \mathbf{r}_1 is expressed as [6]

$$\mathbb{R}(\mathbf{r}, \mathbf{r}_1) = \frac{\mathbf{l}^T(\mathbf{r}) \mathbf{R}^{-1} \mathbf{f}}{\mathbf{l}^T(\mathbf{r}) \mathbf{R}^{-1} \mathbf{l}(\mathbf{r})}. \quad (12)$$

Therefore, substituting (10) into (12), we can finally derive the explicit form of the kernel such that

$$\mathbb{R}(\mathbf{r}, \mathbf{r}_1) = \sqrt{\mathbf{f}^T \mathbf{D}^{-1} \mathbf{f}} \frac{\cos(\mathbf{l}, \mathbf{f} | \mathbf{D}^{-1})}{\left[1 + \tilde{\alpha} \left(1 - \cos^2(\mathbf{l}, \mathbf{f} | \mathbf{D}^{-1})\right)\right]} \quad (13)$$

where $\mathbf{D} = \mathbf{I} + (\sigma_c^2/\sigma_0^2)\mathbf{G}$ and $\tilde{\alpha} = (\sigma_1^2/\sigma_0^2)\mathbf{f}^T \mathbf{D}^{-1} \mathbf{f}$. In (13), the normalized lead field vector is used as \mathbf{l} and the explicit notation of (\mathbf{r}) is omitted for simplicity. The generalized cosine in the metric \mathbf{D}^{-1} is defined such that $\cos^2(\mathbf{l}, \mathbf{f} | \mathbf{D}^{-1}) = (\mathbf{l}^T \mathbf{D}^{-1} \mathbf{f})^2 / [(\mathbf{l}^T \mathbf{D}^{-1} \mathbf{l})(\mathbf{f}^T \mathbf{D}^{-1} \mathbf{f})]$. In Section V-A, we present numerical examples of the resolution kernel obtained using (13). These numerical examples show that when large background activities exist, significant reduction in source intensity, as well as the subsequent degradation of the spatial resolution, arises in source reconstruction results.

IV. PROPOSED PREWHITENING EIGENSPACE BEAMFORMER

A. Definitions

Here, we present the proposed eigenspace beamformer, which can attain the source reconstruction free from the influence of background interference. To describe the method, we first make several definitions. We define the spatio-temporal matrix of the measurement $\mathbf{b}(t)$ as \mathbf{B} such that

$$\mathbf{B} = [\mathbf{b}(t_1), \mathbf{b}(t_2), \dots, \mathbf{b}(t_K)] \quad (14)$$

where t_j ($j = 1, \dots, K$) indicate the time points at which the measurements are performed. The spatio-temporal matrices for $\mathbf{b}_s(t)$ and $\mathbf{b}_I(t)$ are defined in exactly the same manner as in (14), i.e.,

$$\mathbf{B}_s = [\mathbf{b}_s(t_1), \mathbf{b}_s(t_2), \dots, \mathbf{b}_s(t_K)] \quad (15)$$

and

$$\mathbf{B}_I = [\mathbf{b}_I(t_1), \mathbf{b}_I(t_2), \dots, \mathbf{b}_I(t_K)]. \quad (16)$$

Then, corresponding to (4), the relationship

$$\mathbf{B} = \mathbf{B}_s + \mathbf{B}_I + \mathbf{N} \quad (17)$$

holds where \mathbf{N} is the noise matrix defined as $\mathbf{N} = [\mathbf{n}(t_1), \dots, \mathbf{n}(t_K)]$.

We define the covariance matrix of the signal magnetic field generated from the target sources only as \mathbf{R}_s , such that

$$\mathbf{R}_s = \langle \mathbf{b}_s(t) \mathbf{b}_s^T(t) \rangle. \quad (18)$$

We also define the signal-plus-sensor-noise covariance matrix \mathbf{R}_{s+n} , such that

$$\mathbf{R}_{s+n} = \langle [\mathbf{b}_s(t) + \mathbf{n}(t)] [\mathbf{b}_s(t) + \mathbf{n}(t)]^T \rangle \quad (19)$$

and the interference-plus-sensor-noise covariance matrix \mathbf{R}_{i+n} , such that

$$\mathbf{R}_{i+n} = \langle [\mathbf{b}_I(t) + \mathbf{n}(t)] [\mathbf{b}_I(t) + \mathbf{n}(t)]^T \rangle. \quad (20)$$

We further assume that the background interferences are uncorrelated with the target activity. Under this assumption, the relationship

$$\mathbf{R} = \mathbf{R}_s + \mathbf{R}_{i+n} \quad (21)$$

holds. The fundamental assumption in this paper is that control-state measurements, which contain only the contributions from the background interference and sensor noise, are available, and the interference-plus-noise covariance matrix \mathbf{R}_{i+n} can be obtained from such control-state measurements. Under this assumption, we have developed a novel beamformer method, the prewhitening eigenspace beamformer, to extract the target activities from the background interference.

B. Prewhitening Eigenspace Beamformer

The proposed beamformer uses the prewhitened measurement covariance matrix $\tilde{\mathbf{R}}$, which is defined as $\tilde{\mathbf{R}} = \mathbf{R}_{i+n}^{-1/2} \mathbf{R} \mathbf{R}_{i+n}^{-1/2}$. Thus, from (21), we have the relationship

$$\tilde{\mathbf{R}} = \mathbf{R}_{i+n}^{-1/2} \mathbf{R}_s \mathbf{R}_{i+n}^{-1/2} + \mathbf{I}. \quad (22)$$

We define the eigenvalues and eigenvectors of $\tilde{\mathbf{R}}$ as $\gamma_1, \dots, \gamma_M$ and $\mathbf{u}_1, \dots, \mathbf{u}_M$. Because we assume that Q target sources exist, according to (22), the Q largest eigenvalues $\gamma_1, \dots, \gamma_Q$ are greater than 1 and associated with the signal part $\mathbf{R}_{i+n}^{-1/2} \mathbf{R}_s \mathbf{R}_{i+n}^{-1/2}$; and the other eigenvalues $\gamma_{Q+1}, \dots, \gamma_M$

are equal to 1 and are associated with the interference and noise part. That is, $\tilde{\mathbf{R}}$ is expressed as

$$\tilde{\mathbf{R}} = \sum_{j=1}^M \gamma_j \mathbf{u}_j \mathbf{u}_j^T = \sum_{j=1}^Q \gamma_j \mathbf{u}_j \mathbf{u}_j^T + \sum_{j=Q+1}^M \mathbf{u}_j \mathbf{u}_j^T \quad (23)$$

and, thus, we have

$$\mathbf{R}_{i+n}^{-1/2} \mathbf{R}_s \mathbf{R}_{i+n}^{-1/2} = \tilde{\mathbf{R}} - \mathbf{I} = \sum_{j=1}^Q (\gamma_j - 1) \mathbf{u}_j \mathbf{u}_j^T \approx \sum_{j=1}^Q \gamma_j \mathbf{u}_j \mathbf{u}_j^T. \quad (24)$$

Using these signal-level eigenvectors, we define a matrix \mathbf{U}_S as $\mathbf{U}_S = [\mathbf{u}_1, \dots, \mathbf{u}_Q]$, and calculate $\mathbf{U}_S \mathbf{U}_S^T$, which is the projection matrix that project vectors onto the signal subspace of $\tilde{\mathbf{R}}$. Thus, a reasonable estimate of the signal-only covariance matrix, $\hat{\mathbf{R}}_s$, can be obtained using

$$\hat{\mathbf{R}}_s = \mathbf{R}_{i+n}^{1/2} \mathbf{U}_S \mathbf{U}_S^T \tilde{\mathbf{R}} \mathbf{R}_{i+n}^{1/2} = \mathbf{R}_{i+n}^{1/2} \sum_{j=1}^Q \gamma_j \mathbf{u}_j \mathbf{u}_j^T \mathbf{R}_{i+n}^{1/2} \approx \mathbf{R}_s. \quad (25)$$

An estimate of the signal-plus-sensor-noise covariance matrix, $\hat{\mathbf{R}}_{s+n}$, can be obtained from

$$\hat{\mathbf{R}}_{s+n} = \mathbf{R}_{i+n}^{1/2} \mathbf{U}_S \mathbf{U}_S^T \tilde{\mathbf{R}} \mathbf{R}_{i+n}^{1/2} + \mu \mathbf{I} = \hat{\mathbf{R}}_s + \mu \mathbf{I} \quad (26)$$

where μ is the regularization constant that should be set close to the variance of the sensor noise σ_0^2 . The source power reconstruction free from the influence of the background activity can be obtained from

$$\langle \hat{s}(\mathbf{r}, t)^2 \rangle = \frac{1}{\mathbf{l}^T(\mathbf{r}) \hat{\mathbf{R}}_{s+n}^{-1} \mathbf{l}(\mathbf{r})}. \quad (27)$$

A reasonable estimate of the spatio-temporal matrix of the signal magnetic field \mathbf{B}_s can also be obtained in the same manner as described above. The prewhitened version of \mathbf{B} is defined as $\tilde{\mathbf{B}}$ such that

$$\tilde{\mathbf{B}} = \mathbf{R}_{i+n}^{-1/2} \mathbf{B} = \mathbf{R}_{i+n}^{-1/2} \mathbf{B}_s + \mathbf{R}_{i+n}^{-1/2} (\mathbf{B}_I + \mathbf{N}). \quad (28)$$

The singular value decomposition of the $\tilde{\mathbf{B}}$ is expressed as

$$\tilde{\mathbf{B}} = \sum_{j=1}^M \sqrt{\gamma_j} \mathbf{u}_j \mathbf{v}_j^T, \quad (29)$$

where \mathbf{v}_j^T indicates the j th temporal singular vector. Here, again, the first Q singular values are greater than 1 and they are associated with the signal part $\mathbf{R}_{i+n}^{-1/2} \mathbf{B}_s$. The other singular values are close to 1 and they are associated with the interference and noise part $\mathbf{R}_{i+n}^{-1/2} (\mathbf{B}_I + \mathbf{N})$. Therefore, by applying the projector $\mathbf{U}_S \mathbf{U}_S^T$ to $\tilde{\mathbf{B}}$, we have

$$\mathbf{U}_S \mathbf{U}_S^T \tilde{\mathbf{B}} = \sum_{j=1}^Q \sqrt{\gamma_j} \mathbf{u}_j \mathbf{v}_j^T \approx \mathbf{R}_{i+n}^{-1/2} \mathbf{B}_s. \quad (30)$$

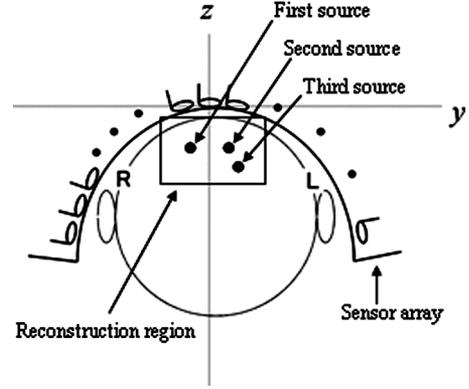


Fig. 1. The coordinate system used in the numerical experiments. The coordinate origin was set at the center of the sensor coil located at the center of the array. The plane at $x = 0$ cm is shown. The coordinate of the upper left, the upper right, and the lower sources are $(0, -1, -6)$, $(0, 1, -6)$, and $(0, -1.6, -7.2)$ cm, respectively. The circle indicates the boundary of the sphere used for the forward calculations. The center of the sphere was set to $(0, 0, -12)$.

Thus, we can extract the spatio-temporal matrix of the signal magnetic field \mathbf{B}_s such that

$$\mathbf{R}_{i+n}^{1/2} [\mathbf{U}_S \mathbf{U}_S^T \tilde{\mathbf{B}}] \approx \mathbf{R}_{i+n}^{1/2} \mathbf{R}_{i+n}^{-1/2} \mathbf{B}_s = \mathbf{B}_s. \quad (31)$$

Defining $\mathbf{\Pi}_S$ such that $\mathbf{\Pi}_S = \mathbf{R}_{i+n}^{1/2} [\mathbf{U}_S \mathbf{U}_S^T] \mathbf{R}_{i+n}^{-1/2}$, we have the relationship,

$$\mathbf{\Pi}_S \mathbf{B} \approx \mathbf{B}_s \quad (32)$$

and the weight vector of the prewhitening eigenspace beamformer is expressed as

$$\mathbf{w}_p(\mathbf{r}) = \frac{\mathbf{\Pi}_S \hat{\mathbf{R}}_{s+n}^{-1} \mathbf{l}(\mathbf{r})}{\mathbf{l}^T(\mathbf{r}) \hat{\mathbf{R}}_{s+n}^{-1} \mathbf{l}(\mathbf{r})} \quad (33)$$

and the interference-free spatio-temporal source reconstruction is obtained using this $\mathbf{w}_p(\mathbf{r})$, i.e.,

$$\begin{aligned} [\hat{s}(\mathbf{r}, t_1), \dots, \hat{s}(\mathbf{r}, t_K)] &= \mathbf{w}_p^T(\mathbf{r}) \mathbf{B} \\ &= \frac{\mathbf{l}^T(\mathbf{r}) \hat{\mathbf{R}}_{s+n}^{-1} \mathbf{\Pi}_S \mathbf{B}}{\mathbf{l}^T(\mathbf{r}) \hat{\mathbf{R}}_{s+n}^{-1} \mathbf{l}(\mathbf{r})} \\ &= \frac{\mathbf{l}^T(\mathbf{r}) \hat{\mathbf{R}}_{s+n}^{-1} \mathbf{B}_s}{\mathbf{l}^T(\mathbf{r}) \hat{\mathbf{R}}_{s+n}^{-1} \mathbf{l}(\mathbf{r})}. \end{aligned} \quad (34)$$

V. NUMERICAL EXPERIMENTS

A. Numerical Examples of Resolution Kernel

A sensor alignment of the 148-sensor array from Magnes 2500 (4D Neuroimaging Inc., San Diego) neuromagnetometer is used in our experiments. Three signal sources were assumed to exist on a single plane ($x = 0$ cm). The source-sensor configuration and the coordinate system are illustrated in Fig. 1, and the spherical homogeneous conductor model is used for the

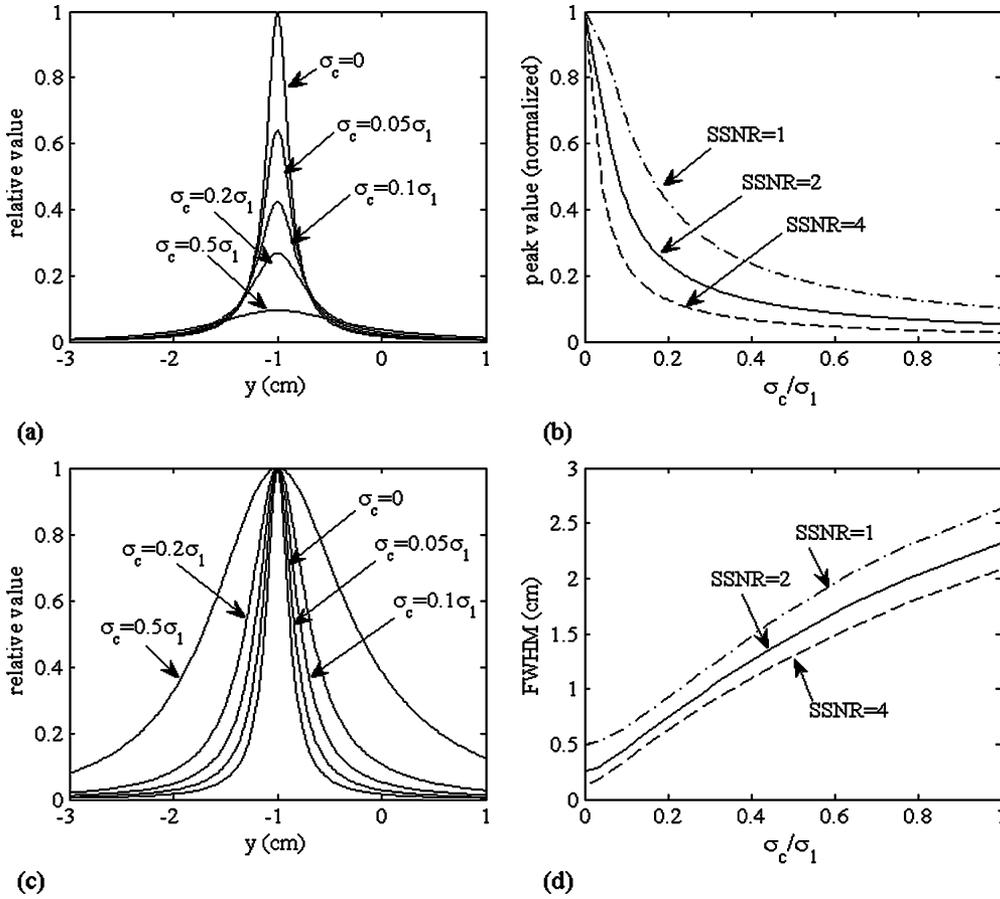


Fig. 2. (a) Resolution kernels of the upper-left source located at $(0, -1, -6)$ cm. Five values of σ_c were used: $\sigma_c = 0$, $\sigma_c = 0.05\sigma_1$, $\sigma_c = 0.1\sigma_1$, $\sigma_c = 0.2\sigma_1$, and $\sigma_c = 0.5\sigma_1$. The SSNR, which is defined as $(\sigma_1\|\mathbf{f}\|)/(\sigma_0\sqrt{M})$, was set to 2. (b) Plot of the peak value of the kernel, $\mathbb{R}(\mathbf{r}_1, \mathbf{r}_1) = \sqrt{\mathbf{f}^T \mathbf{D}^{-1} \mathbf{f}}$, with respect to σ_c for three SSNR values. (c) The same resolution kernels as shown in (a) in which each kernel is normalized with its peak value. (d) Plot of the FWHM of the resolution kernel with respect to σ_c for three SSNR values.

forward calculation. We here assume that only the upper-left source is active; the source is located 6 cm below the center of the sensor array ($\mathbf{r}_1 = (0, -1, -6)$ cm). We calculated the resolution kernel using (13) for five values of σ_c/σ_1 . Here, the signal-to-sensor-noise ratio (SSNR), which is defined as $(\sigma_1\|\mathbf{f}\|)/(\sigma_0\sqrt{M})$, was set equal to 2. Also, in this calculation, the gram matrix \mathbf{G} is approximated as

$$\mathbf{G} = \sum_j \mathbf{l}_\theta(\mathbf{r}_j)\mathbf{l}_\theta^T(\mathbf{r}_j) + \mathbf{l}_\phi(\mathbf{r}_j)\mathbf{l}_\phi^T(\mathbf{r}_j)$$

where $\mathbf{l}_\theta(\mathbf{r}_j)$ and $\mathbf{l}_\phi(\mathbf{r}_j)$ are the lead field vectors in the directions of the two tangential components, and \mathbf{r}_j is the coordinate of the j th voxel. Here, the voxel grid has 0.5-cm interval within a volume defined as $-8 \leq x \leq 8$, $-8 \leq y \leq 8$, and $-11 \leq z \leq -3$.

The results plotted in Fig. 2(a) show that, when the power of the background activity, σ_c^2 , is increased, the reconstructed intensity of the source rapidly decreases. The peak value of the resolution kernel $\mathbb{R}(\mathbf{r}_1, \mathbf{r}_1) = \sqrt{\mathbf{f}^T \mathbf{D}^{-1} \mathbf{f}}$ was plotted with respect to σ_c/σ_1 in Fig. 2(b) for the three values of SSNR. These plots show that large background activities such as those with $\sigma_c = 0.5\sigma_1$ can cause a more than 70% decrease in the reconstructed intensity, and that this decrease is more significant when the SSNR is greater. The same resolution kernels in Fig. 2(a) are plotted in Fig. 2(c) where each kernel was normalized with

its peak value. These normalized kernels clearly show that the full-width at half-maximum (FWHM) of the kernels becomes greater when σ_c is increased. The FWHM of the resolution kernels is plotted with respect to σ_c/σ_1 for three different values of the SSNR. The results show that, compared to a case where background interferences are negligibly small, a large spatial blur can be caused by background activities such as those with $\sigma_c > 0.5\sigma_1$.

B. Source Reconstruction Experiments

We then performed source reconstruction experiments to validate the effectiveness of the prewhitening beamformer proposed in Section IV. Simulated magnetic recordings were calculated from -1200 to 1200 time points by assigning the three time courses shown in Fig. 3(a) to the three sources. We use the spherically homogeneous conductor model [10] for the forward calculation. In these numerical experiments, we consider the data portion between -1200 and 0 to be the prestimulus period and that between 0 and 1200 to be the poststimulus period. A small amount of white Gaussian noise that simulates the sensor noise was added to the generated recordings, resulting in a SSNR equal to 12, where the SSNR is estimated using the ratio between the Frobenius norms of the signal and noise matrices, i.e., $\|\mathbf{B}_s\|/\|\mathbf{N}\|$. The generated magnetic recordings $\mathbf{B}_s + \mathbf{N}$ are shown in the upper panel of Fig. 3(b). We then generated the magnetic field due to the background interference \mathbf{B}_I . In this

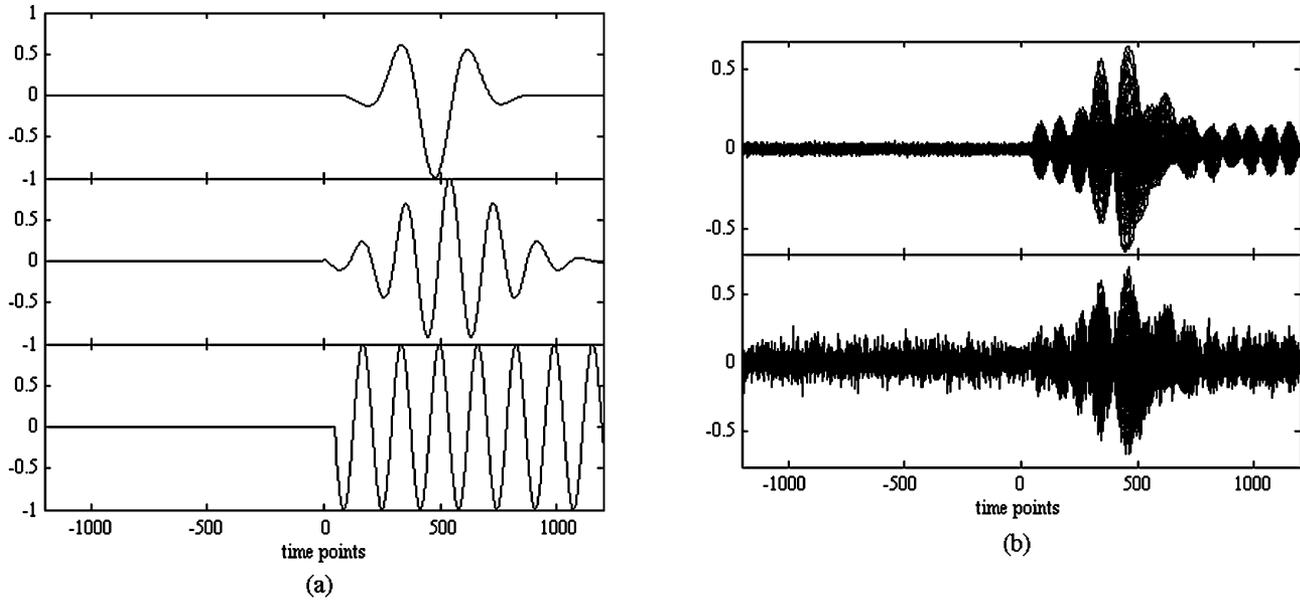


Fig. 3. (a) Waveforms of the three sources assumed for the numerical experiments. The waveforms in the top to the bottom panels were assigned to the first to third sources, respectively. (b) Generated magnetic recordings obtained when no background sources exist (upper panel), and when 100 background sources exist (lower panel).

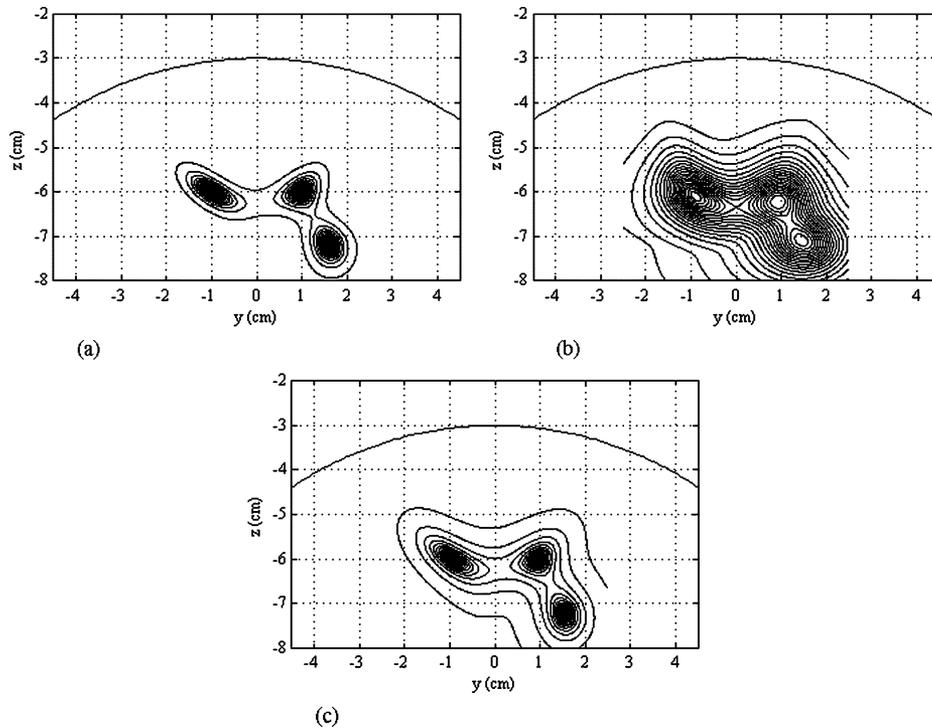


Fig. 4. Results of the power reconstruction $\langle \hat{s}(\mathbf{r}, t)^2 \rangle$. (a) Conventional eigenspace beamformer was applied to the recordings with no background interference. (b) Conventional eigenspace beamformer was applied to the recordings with background interference. (c) Prewhitening beamformer reconstruction [see (27)] was applied to the recordings with background interference. In these results, the reconstruction grid has 0.1-cm intervals in the y and z directions.

generation, 100 background sources with random locations and orientations had the same power and random time courses. The background magnetic field \mathbf{B}_I was added to $\mathbf{B}_s + \mathbf{N}$ and the resultant simulated magnetic recordings \mathbf{B} are shown in the lower panel of Fig. 3(b). Here, the resultant interference-to-signal ratio $\|\mathbf{B}_s\|/\|\mathbf{B}_I\|$ was set equal to 2.

The conventional eigenspace beamformer mentioned in Section II-B was first applied to these two sets of simulated recordings in Fig. 3(b). Here, \mathbf{R} was obtained using the

whole poststimulus period, and (2) was used to obtain the source-power reconstruction $\langle \hat{s}(\mathbf{r}, t)^2 \rangle$. Fig. 4(a) shows the results for the case with no background interference, and Fig. 4(b) shows the results for the case with the background interference present. Here, the comparison between these two sets of results again confirms that the background interference causes a severe blur in the reconstruction results. We then applied the prewhitening beamformer in (27) to the data with the background interference. The results are shown in Fig. 4(c).

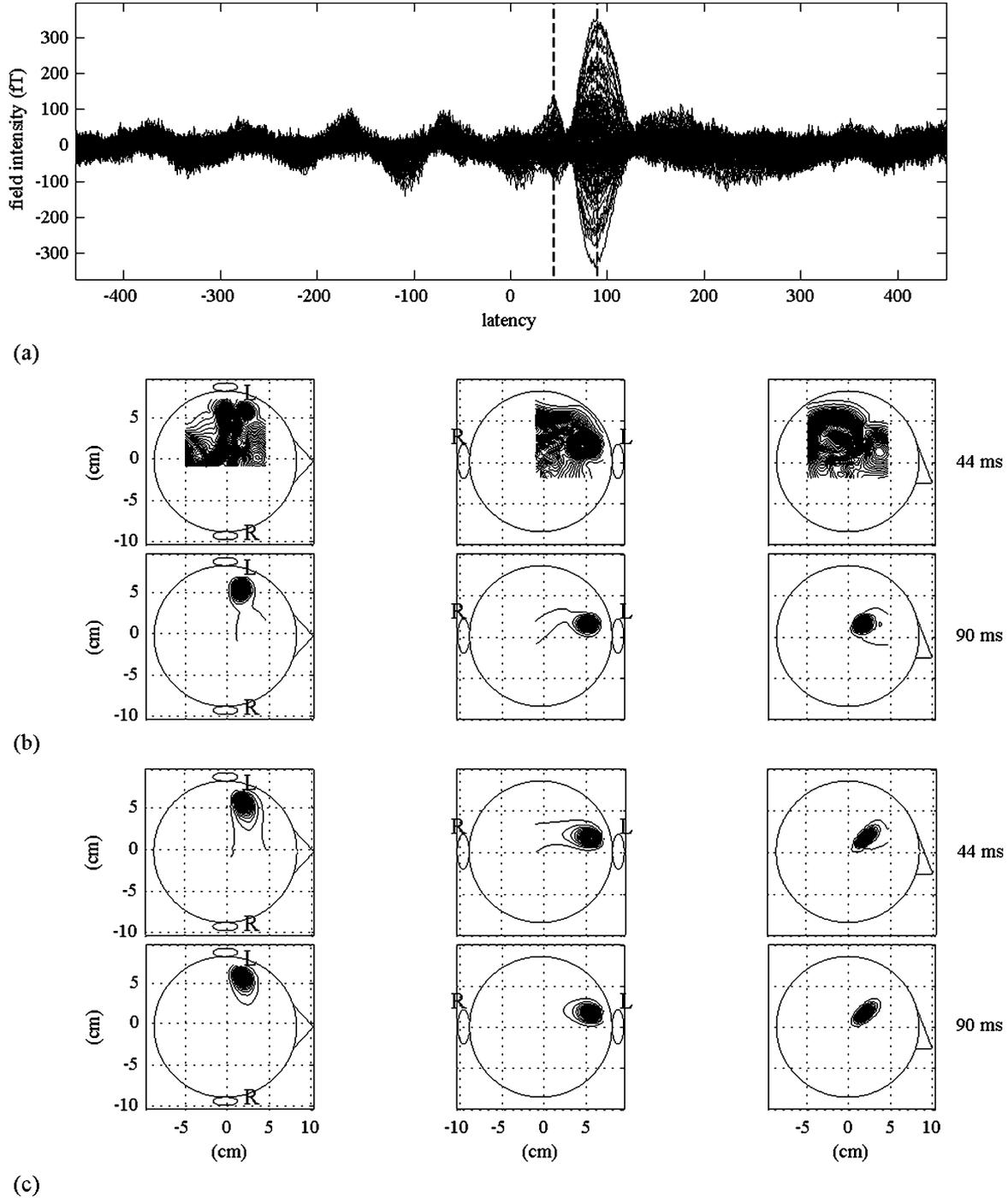


Fig. 5. (a) Averaged auditory-evoked field measured using the 275-channel sensor array. Among the 275 sensor recordings, the recordings from 132 sensors covering the subject's left hemisphere are displayed. Two vertical broken lines indicate the time instants 44 and 90 ms. (b) The source reconstruction results obtained using the conventional eigenspace beamformer. (c) Those from the proposed prewhitening beamformer. The left, middle, and right columns show the maximum intensity projections of the 3-D reconstruction onto the axial, coronal, and sagittal planes, respectively. The upper case letters L and R show the left and the right hemispheres, respectively. The upper and lower panels indicate the reconstruction results at 44 and 90 ms, respectively. In these reconstruction results, the reconstruction grid has 0.5-cm intervals in the x , y , and z directions.

In this application, \mathbf{R}_{i+n} was obtained using the whole prestimulus period. In the results in Fig. 4(c), the blur due to the background activity is significantly reduced, and these results clearly demonstrate the effectiveness of the proposed beamformer.

VI. EXPERIMENTS

We applied the proposed prewhitening beamformer to two sets of MEG data, measured using the 275-channel

Omega-275 (VSM MedTech Ltd., Port Coquitlam, BC, Canada) whole-cortex biomagnetometer installed at the Biomagnetic Imaging Laboratory, University of California, San Francisco. The first data set is the auditory evoked response, and we applied the proposed prewhitening beamformer to demonstrate its capability of spatio-temporal reconstruction free from the influence of background interference. The second data set is the movement-related desynchronization induced by button-press

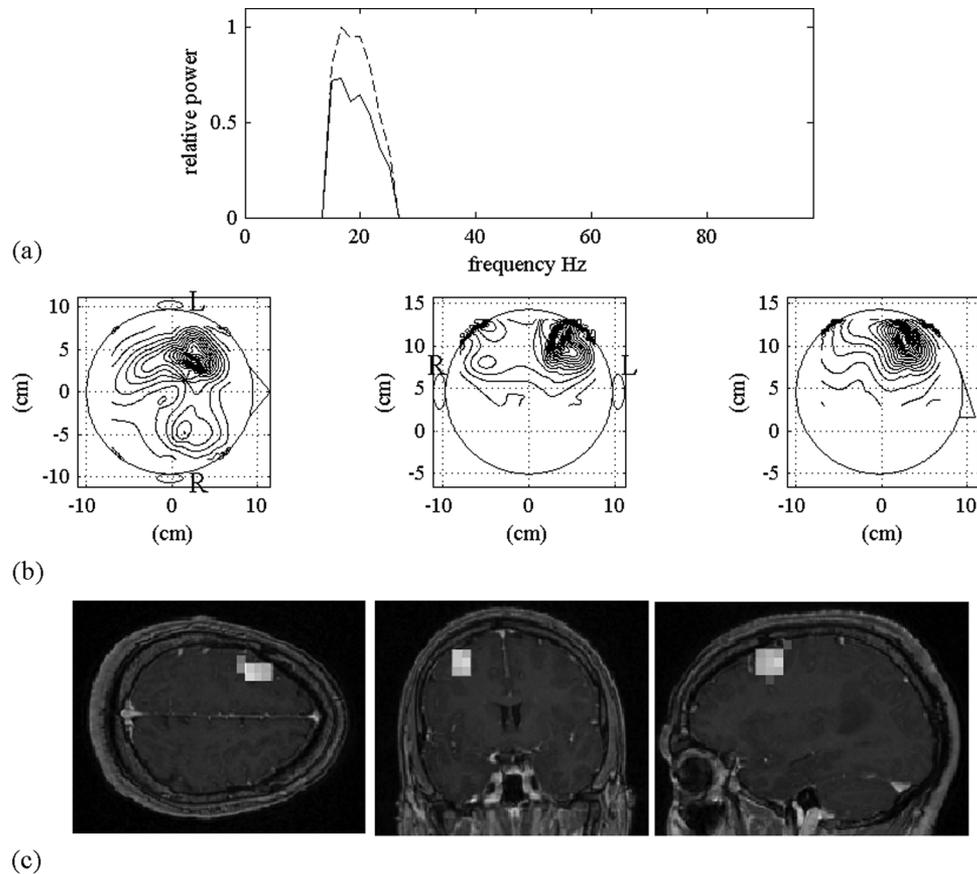


Fig. 6. (a) The power spectra $P_1(f)$ and $P_2(f)$ for the frequency band between 15 and 25 Hz. $P_1(f)$ is indicated by the broken line and $P_2(f)$ by the solid line. (b) The maximum-intensity projection of the power reconstruction $\langle \hat{s}(\mathbf{r}, t)^2 \rangle$ obtained using the prewhitening beamformer in (27). (c) The MRI overlay of the reconstruction results in (b).

finger movements, and we show that the method can reconstruct a clear, localized activity near the hand-motor area, demonstrating that the proposed method is effective for reconstructing nontime-locked brain activities.

A. Application to Auditory-Evoked Data

The auditory-evoked field was measured with a 1-kHz pure tone presented to the subject's right ear. The average inter-stimulus interval was 2 s, with the interval randomly varied between 1.75 and 2.25 s. The sampling frequency was set at 4 kHz, and an on-line filter with a bandwidth from 1 to 2 kHz was used. A total of 400 epochs were measured and averaged to produce the averaged auditory recordings shown in Fig. 5(a). Here, although clear P50m and N100m peaks can be observed, we can see that these averaged recordings contain a considerable amount of quasi-periodic background activity.

The reconstruction experiments were performed using the conventional eigenspace-projected beamformer and the proposed prewhitening beamformer. In these experiments, the left hemisphere was reconstructed using the averaged recordings from 132 sensors covering the left hemisphere. [Only the recordings from these 132 sensors are displayed in Fig. 5(a).] A portion of the averaged recordings between 0 to 200 ms was used to estimate the measurement covariance matrix \mathbf{R} , and the interference-plus-noise covariance \mathbf{R}_{i+n} was obtained from the whole prestimulus portion between -400 and 0 ms. Two time points, 44 and 90 ms, are selected for the result comparison. These time points are shown in the two vertical broken lines in

Fig. 5(a), and as indicated, one is near the peak vertex of P50m and the other is near the peak vertex of N100m.

The conventional eigenspace-projected beamformer in (1) and (3) was first applied to these averaged recordings. The source reconstruction results at the two time points are shown in Fig. 5(b). The results from the prewhitening beamformer, obtained using (34), are shown in Fig. 5(c). The dimension of the signal subspace was set to 2 for the both cases. At 90-ms latency, which is close to the peak vertex of N100m, both methods can reconstruct a clear localized source in the left temporal lobe probably near the primary auditory area. However, at 44 ms, the reconstruction results of the conventional eigenspace beamformer contain a strong diffuse source, probably caused by the background brain activity. The results from the prewhitening beamformer are free from this diffuse source and clearly detect a localized source in the left temporal lobe, demonstrating the effectiveness of the proposed prewhitening beamformer.

B. Application to Movement-Related Desynchronization Data

Here, a subject was asked to press a button with his right-index finger every 3–4 s. The onset of movement was indicated by a button press and defined as the time-origin. MEG data for 200 button presses were continuously acquired at a 1 kHz sampling rate. Because movement-induced magnetic fields are not precisely phase locked to the movement, we estimated the covariance matrices from the raw epoched data. Since, the raw epoch data will be contaminated by background interferences,

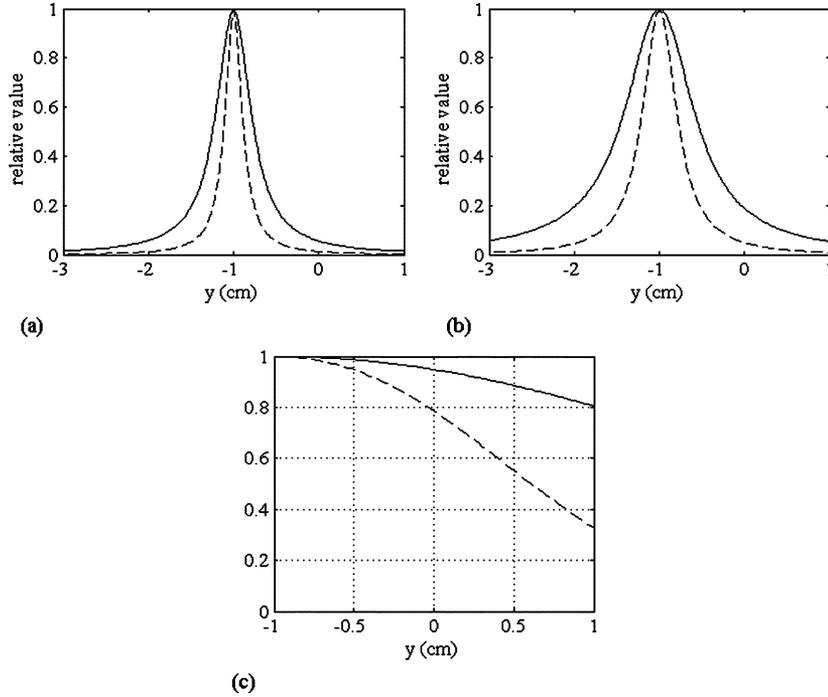


Fig. 7. Comparison between the point spread functions in (36) and (37). The solid lines indicate the point spread function in (36) and the broken lines indicate that in (37). The value of α in (36) and the value of α' in (37) were set equal. (a) These values were set to 1, and (b) 0.5. (c) Plot of $\cos(\mathbf{l}, \mathbf{f})$ (solid line) and $\cos(\mathbf{l}, \mathbf{f}|\mathbf{G}^{-1})$ (broken line). These generalized cosines were calculated on the line $x = 0, z = -6$ and $-1 \leq y \leq 1$ cm.

we applied our proposed prewhitening beamformer. It is well-known that the spectrum of the magnetic field decreases in the beta-band (15–25 Hz) preceding movement [11]. Therefore, covariance estimates were obtained in the frequency domain.

We set two time windows for covariance matrix estimation: the first from -1200 to -600 ms, and the second from -600 to 0 ms, both preceding the button press. Fourier transforms of the k th nonaveraged epoch data in the first and the second time windows are, respectively, denoted $\mathbf{g}_1^k(f)$ and $\mathbf{g}_2^k(f)$, and the frequency-domain sample covariance matrices for the first and the second time windows, $\hat{\mathbf{\Omega}}_1$ and $\hat{\mathbf{\Omega}}_2$, are obtained using

$$\hat{\mathbf{\Omega}}_j = \sum_{f \in F_w} \sum_{k=1}^{200} \mathbf{g}_j^k(f) (\mathbf{g}_j^k(f))^T \quad (35)$$

where $j = 1$ and 2 . In this equation, the notation $\sum_{f \in F_w}$ indicates the summation over a specific frequency band F_w , and F_w was set to the β -band region between 15 and 25 Hz in our experiments. The power spectra averaged across channels, $P_1(f)$ and $P_2(f)$, were also calculated for the first and the second time windows such that $P_j(f) = (1/M) \sum_{k=1}^{200} \|\mathbf{g}_j^k(f)\|^2$ where $j = 1, 2$. The power spectrum $P_1(f)$ for the frequency band F_w ($15 \leq f \leq 25$ Hz) is plotted by the broken line and $P_2(f)$ by the solid line in Fig. 6(a). These plots indicate that $P_1(f)$ is larger than $P_2(f)$ in this frequency band, confirming the movement-related desynchronization. Consequently, $\hat{\mathbf{\Omega}}_1$ is used as the target covariance matrix, and $\hat{\mathbf{\Omega}}_2$ as the interference-plus-noise covariance matrix.

We applied the prewhitening beamformer to obtain the source power reconstruction $\langle \hat{s}(\mathbf{r}, t)^2 \rangle$. The reconstruction results are shown in Fig. 6(b). We can see that the proposed method reconstructs a clear, localized source in the left temporal region. The

MRI overlay of the results in Fig. 6(b) is shown in Fig. 6(c). The overlay shows that the center of the reconstructed activity is located in contralateral hand-motor cortex. The results in Fig. 6(b) and (c) demonstrate the capability of the proposed beamformer to successfully reconstruct the nontime-locked source activity by eliminating the influence of background interference.

VII. DISCUSSION AND CONCLUSION

The analysis and numerical experiments in Sections III and V-A show that the background interference causes blurred reconstruction. On the other hand, the sensor noise is known to cause the degradation in the spatial resolution [12]. Let us compare the effects of these two types of noise on the spatial resolution. When the background interference is negligibly small, substituting (10) with $\sigma_c = 0$ into (12), we derive the kernel in this case as

$$\mathbb{R}(\mathbf{r}, \mathbf{r}_1) = \frac{\cos(\mathbf{l}, \mathbf{f}|\mathbf{I})}{[1 + \alpha(1 - \cos^2(\mathbf{l}, \mathbf{f}|\mathbf{I}))]} = \frac{\cos(\mathbf{l}, \mathbf{f})}{[1 + \alpha(1 - \cos^2(\mathbf{l}, \mathbf{f}))]} \quad (36)$$

where α is defined such that $\alpha = (\sigma_1^2/\sigma_0^2)\|\mathbf{f}\|^2$, and $\cos^2(\mathbf{l}, \mathbf{f}|\mathbf{I})$ is denoted $\cos^2(\mathbf{l}, \mathbf{f})$. The SSNR is expressed using α as α/\sqrt{M} . In (36), a multiplicative constant is omitted and the peak value is normalized to 1. When the power of background interference is much larger than the power of sensor noise, substituting $\mathbf{D} \approx (\sigma_c^2/\sigma_0^2)\mathbf{G}$ into (13), we derive

$$\mathbb{R}(\mathbf{r}, \mathbf{r}_1) = \frac{\cos(\mathbf{l}, \mathbf{f}|\mathbf{G}^{-1})}{[1 + \alpha'(1 - \cos^2(\mathbf{l}, \mathbf{f}|\mathbf{G}^{-1}))]} \quad (37)$$

where α' is defined such that $\alpha' = (\sigma_1^2/\sigma_c^2)(\mathbf{f}^T \mathbf{G}^{-1} \mathbf{f})$. We define the signal-to-interference ratio (SIR) as α'/\sqrt{M} , and a multiplicative constant is again omitted in (37).

The results of plotting the point spread functions in (36) and (37) are shown in Fig. 7(a) and (b). Here, α in (36) and α' in (37) were set equal; these values were set to 1 in Fig. 7(a) and to 0.5 in Fig. 7(b). These calculated results show that the FWHM of the point spread function in (36) is approximately twofold greater than that for the point spread function in (37). That is, the blur caused by the sensor noise is twofold greater than that caused by the interference. The difference between the two point spread functions is caused by the difference between $\cos(\mathbf{l}, \mathbf{f})$ and $\cos(\mathbf{l}, \mathbf{f} \mathbf{G}^{-1})$. The decay properties of these generalized cosines are shown in Fig. 7(c), and we can see that $\cos(\mathbf{l}, \mathbf{f} \mathbf{G}^{-1})$ decays twice as fast as $\cos(\mathbf{l}, \mathbf{f})$, thus explaining the difference in these two types of point spread functions.

In summary, this paper proposes a novel prewhitening beamformer, which can achieve source reconstruction free from the influence of background brain activities. The prerequisite for the method is that control-state measurements, which contain only the contributions from the background interference, be available, and that the covariance matrix of the background interference can be obtained from such control-state measurements. The proposed method uses this interference covariance matrix to suppress the influence of the interference in the source reconstruction results. The proposed method is validated by our computer simulation, as well as by applications to two kinds of MEG data.

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